# II B. Tech I Semester Supplementary Examinations, May/June - 2016 MATHEMATICAL FOUNDATIONS OF COMPUTER SCIENCE AND ENGINEERING 

 (Com. to CSE, IT, ECC)Time: 3 hours
Max. Marks: 70

Note: 1. Question Paper consists of two parts (Part-A and Part-B)<br>2. Answer ALL the question in Part-A<br>3. Answer any THREE Questions from Part-B

PART-A

1. a) Prove that $\ulcorner(\mathbf{p} \mathbf{q}) \mathbf{v}[(\ulcorner\mathbf{p}) \boldsymbol{\Lambda} \mathbf{q}] \mathbf{v p}$ is a tautology using truth table?
b) Write the statement of Euler's theorem and explain with an example?
c) Draw hasse diagram of $[\mathbf{P}(\{\mathbf{a}, \mathbf{b}, \mathbf{c}\}) ; \subseteq]$ ?
d) What is Hamiltonian graph? Explain with an example?
e) How many $\mathbf{2}$-digit or $\mathbf{3}$-digit numbers can be formed using digits $\mathbf{1 , 4 , 5 , 6 , 8}$ and $\mathbf{9}$ if no repetition is allowed?
f) Explain the method of characteristic roots?
$(4 \mathrm{M}+3 \mathrm{M}+3 \mathrm{M}+4 \mathrm{M}+4 \mathrm{M}+4 \mathrm{M})$

## PART-B

2. a) Verify the validity of the following argument: Lions are dangerous animals, There are lions, There are dangerous animals.
b) What is meant by tautology, contradiction give some example formulas?
( $8 \mathrm{M}+8 \mathrm{M}$ )
3. a) Prove by mathematical induction that $\mathbf{6}^{\mathbf{n + 2}}+\mathbf{7}^{\mathbf{2 n + 1}}$ is divisible by $\mathbf{4 3}$ for each positive integer n ?
b) State and explain Euclidean algorithm with example?
( $8 \mathrm{M}+8 \mathrm{M}$ )
4. a) $R$ is a reflexive relation on set $\mathbf{A}$, prove or disprove $\mathbf{R} \cdot \mathbf{R}^{-1}$ is transitive?
b) Find the transitive closure of $\mathbf{R}$ if
(i) $\mathbf{R}=\{(\mathbf{a}, \mathbf{b}),(\mathbf{b}, \mathbf{c}),(\mathbf{c}, \mathbf{d}),(\mathbf{d}, \mathbf{e})\}$
(ii) $\mathbf{R}=\{(\mathbf{a}, \mathbf{a}),(\mathbf{a}, \mathbf{b}),(\mathbf{b}, \mathbf{c}),(\mathbf{b}, \mathbf{d}),(\mathbf{d}, \mathbf{c}),(\mathbf{d}, \mathbf{d})\}$
( $8 \mathrm{M}+8 \mathrm{M}$ )
5. a) Write about Preorder ,Postorder ,Inorder traversals of tree with examples?
b) Show that any graph with $\mathbf{4}$ or fewer vertices is planar?
6. a) Explain the properties of Cosets with examples?
b) Verify that $\mathbf{C}(\mathbf{n} \mathbf{+ 2 , r}) \mathbf{- 2} \mathbf{C}(\mathbf{n}+\mathbf{1}, \mathbf{r})+\mathbf{C}(\mathbf{n}, \mathbf{r})=\mathbf{C}(\mathbf{n}, \mathbf{r}-\mathbf{2})$
7. a) Solve the recurrence relation of the sequence of numbers $\mathbf{f}_{\mathrm{n}}=\mathbf{f}_{\mathrm{n}-1}+\mathbf{f}_{\mathrm{n}-2}, \mathbf{n}>=\mathbf{2}$ With the initial condition $\mathbf{f}_{\mathbf{0}}=\mathbf{1 ,}, \mathbf{f}=\mathbf{1}$.
b) What is a Generating function and explain the operations on generating functions? $(8 \mathrm{M}+8 \mathrm{M})$
