

DESIGN OF TWO-WAY SLAB

→ * Design a RC slab for a room of size $5.5\text{ m} \times 4\text{ m}$ clear dimensions & carrying a super imposed load of intensity 4 kN/m^2 . Use M_{20} grade concrete HYSD steel; all the four edges are simply supported with corners held down?

Sol: Given data

* Intensity of live load on slab = 4 kN/m^2

* Grade of concrete = M_{20}

* Grade of steel = Fe_{415}

* Length of the slab $l_y = 5.5\text{ m}$

* Width of the slab $l_x = 4\text{ m}$

$$\rightarrow l_y/l_x = \frac{5.5}{4} = 1.375 \quad [< 2]$$

* Since $l_y/l_x < 2$, the slab is to be designed as the TWO-WAY SLAB.

→ STEP: ① Calculation of design loads on slab.

* Assume intensity of dead load due to slab and imposed floor finish as 5 kN/m^2 * [ANNEX-D]

* Considering a strip of unit width, along the [parallel to] the width of the slab in accordance with Appendix 'D' of IS: 456-2000 for the calculation of design load.

* Assuming an effective depth of slab 120 mm with an effective cover of 20 mm [overall depth = 140 mm], the effective length of the slab

in both directions are as follows.

0.0835

* The effective length along 'x' direction

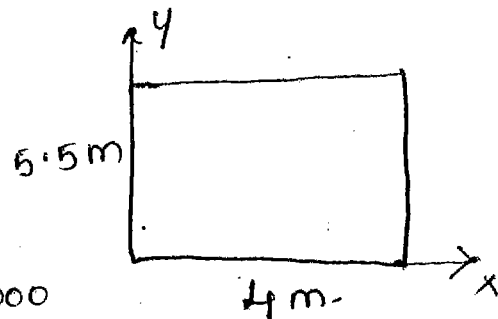
$$L_x = 4 + 0.12 = 4.12 \text{ m.}$$

* The effective length along 'y' direction

$$L_y = 5.5 + 0.12 = 5.62 \text{ m.}$$

→ Design Bending Moments:

[Table 26]



According to D-1.1 of IS: 456-2000

the design bending moment expressions for slabs spanning in two directions are

$$M_x = \alpha_x W L_x^2$$

$$M_y = \alpha_y W L_x^2$$

Where W = Total factored intensity of UDL along short span direction per meter.

$$= 1.5 [W_D + W_L] \times 1$$

$$= 1.5 [5 + 4] \times 1 = 13.5 \text{ kN/m}$$

$$L_x = 4.12 \text{ m.}$$

$$\alpha_x = 0.0835$$

$$\alpha_y = 0.056$$

Refer Table 26 of ANNEX D

Case: No. (9). IS: 456-2000.

$$\therefore M_x = 0.0835 [13.5] [4.12]^2$$

$$= 19.13 \text{ kN-m/m.}$$

$$M_y = 0.056 [13.5] [4.12]^2$$

$$= 12.83 \text{ KN-m/m}$$

→ Design Shear force:

$$\frac{WL}{2} = \frac{13.5 \times 4.4}{2} = 29.7 \text{ KN}$$

→ STEP: ② Determination of Required depth of slab:
[ANNEX: G]

$$* M_u = M_{u\text{lim}} = 0.138 f_{ck} b d^2$$

$$\therefore d_{\text{req}} = \sqrt{\frac{M_u}{0.138 f_{ck} b}}$$

$$\Rightarrow d_{\text{req}} = \sqrt{\frac{19.13 \times 10^6}{0.138 \times 20 \times 1000}}$$

$$\Rightarrow d_{\text{req}} = 83.25 \text{ mm} \ll [< 120 \text{ mm}] \text{ Hence OK}$$

* From clause 24.1 of IS: 456-2000 pg-39

$$L_x/d \leq 35 \times 0.8 = 28$$

$$\therefore d_{\text{req}} \geq \frac{4120}{28} = \frac{4000}{28} = 142.85 \text{ [} > 120 \text{ mm]}$$

∴ Revise the effective depth of the slab as 145 mm with an effective cover 20 mm [overall depth 165 mm]

→ STEP: ③ Design for flexure: [ANNEX: G & D]

→ Positive moment reinforcement along short span:

$$M_{ux} = 0.87 f_y A_{st} d \left[1 - \frac{f_y A_{st}}{f_{ck} b d} \right]$$

$$\Rightarrow 19.13 = 0.87 \times 415 \times A_{st} \times 145 \left[1 - \frac{415 A_{st}}{20 \times 1000 \times 145} \right]$$

$$\Rightarrow \cancel{19.13} = \cancel{52.35 \times 10^3} A_{st} \left[1 - \cancel{148.1 \times 10^{-6}} A_{st} \right]$$

$$\Rightarrow \cancel{19.13} = \cancel{52.35 \times 10^3} A_{st} - \cancel{7.49} A_{st}^2$$

$$\Rightarrow A_{st} = 386.82 \text{ mm}^2$$

* Spacing required = $S_{req} = \frac{1000 A_{\phi}}{A_{st}}$ [Assume 10 mm bars]

$$\Rightarrow S_{req} = \frac{1000 \times 78.5}{386.82}$$

$$\Rightarrow S_{req} = 202.93 \text{ mm}$$

* provide 10 mm bars @ 150 mm c/c parallel to short span with a clear cover of 20 mm.

$$\text{* provided } A_{st} = \frac{1000 A_{\phi}}{S_{prov}} = \frac{1000 \times 78.5}{150} = 523.33 \text{ mm}^2$$

[> 386 mm²]

→ Positive moment reinforcement along long span: ^{OK}

$$M_{uy} = 0.87 f_y A_{st} d \left[1 - \frac{f_y A_{st}}{f_{ck} b d} \right]$$

$$\Rightarrow \cancel{12.83} = \cancel{0.87} \times \cancel{415} \times$$

effective depth of slab along long span direction

$$d_y = 145 - 10 = 135 \text{ mm}$$

$$\therefore 12.83 = 0.87 \times 415 \times A_{st} \times 135 \left[1 - \frac{415 \times A_{st}}{20 \times 1000 \times 135} \right]$$

$$\Rightarrow A_{st} = 274.83 \text{ mm}^2$$

$$* \text{ Spacing required} = S_{req} = \frac{1000 A_{\phi}}{A_{st}} \quad [\text{Assume 8 mm bars}]$$

$$\Rightarrow S_{req} = \frac{1000 \times 50.5}{274.83} = 183.74 \text{ mm}$$

\(\therefore\) provide 8 mm dia bars @ 150 mm c/c parallel to long span with a clear cover of 30 mm.

$$* \text{ provide } A_{st} = \frac{1000 A_{\phi}}{S_{prov}} = \frac{1000 \times 50.5}{150} = 336.6 \text{ mm}^2$$

$$[> 274.83]$$

OK//

\(\rightarrow\) Minimum Reinforcement:

[clause 26.5.2]

$$* \text{ Minimum reinforcement area} = \frac{0.12}{100} \times b \times D = 198 \text{ mm}^2$$

$$\text{Hence } \begin{cases} x < 523.33 \text{ mm}^2 \\ y < 336.6 \text{ mm}^2 \end{cases}$$

* Corner reinforcement [ANNEX D - D.18]

* Area of corner reinforcement required

$$= \frac{3}{4} A_{st} \text{ along short span direction}$$

$$= \frac{3}{4} \times 386.82 = 290.11 \text{ mm}^2$$

$$* \text{ Assume 8 mm bars, Spacing req} = \frac{L_x}{5} \times A_{\phi}$$

$$= 143.43 \text{ mm}$$

\(\therefore\) provide 8 mm dia bars @ 100 mm c/c in 4 layers at

Each corner of the slab with is a distance equal to $l_x/5 = 825 \text{ mm}$.

→ STEP: ④ Check for Shear [clause: 40]

* Design shear force $V_u = 29.7 \text{ kN}$.

* Nominal shear stress $\tau_v = \frac{V_u}{bd} = \frac{29.7 \times 10^3}{1000 \times 145}$
 $= 0.20 \text{ mpa}$

* Maximum shear capacity $\tau_{c, \max} = 2.8 \text{ mpa}$ [T-20]

$$\tau_v < \tau_c \text{ [Hence ok]}$$

$$P_t = 100 \frac{A_{st}}{bd} = \frac{100 \times 523 \times 0.5}{1000 \times 145} = 0.18\%$$

* Design shear strength [T-19, IS:456-2000]

$$\tau_c = 0.304$$

from Table-18, the value of k for a depth of 165 mm slab is 1.27.

$$\therefore \tau_c' = k \times \tau_c = 1.27 \times 0.304 = 0.38 \text{ mpa}$$

$$\therefore \tau_v < \tau_c' \text{ [Hence ok]}$$

\therefore The slab is safe in shear

→ STEP: ⑤ Check for Development length: [cl: 26.2]

$$L_d \leq 1.3 \frac{M}{V} + l_0 \text{ where } L_d = \text{Development length}$$
$$= \frac{\phi \times \sigma_s}{4 \times \tau_{bd}}$$
$$= \frac{\phi \times 0.87 \times 415}{4 \times 1.2 \times 1.6} = 47 \phi$$

$$* M = 0.87 f_y A_{st} d \times \left[1 - \frac{f_y A_{st}}{f_{ck} b d} \right]$$

$$= 0.87 \times 415 \times \frac{523}{2} \times 145 \times \left[1 - \frac{415 \times \frac{523}{2}}{20 \times 1000 \times 145} \right]$$

$$\Rightarrow M = 13.17 \text{ N-mm}$$

$$* V = 29.7 \times 10^3 \text{ N}$$

$$* \text{Initially } l_0 = 0$$

$$\therefore 47 \phi \leq 1.3 \frac{(13.17)}{29.7 \times 10^3} + 0$$

$$\Rightarrow \phi \leq 12.26 \text{ mm } [> 10 \text{ mm}] \text{ Hence ok.}$$

\therefore The slab is safe in Development length.

STEP: ⑥ Check for deflection: [cl: 23.2]

$$l/d \leq k_1 \times k_2 \times k_3 \times k_4 \times k_5$$

$$\text{Where } L = L_x = 4000 \text{ mm.}$$

$$d = 145 \text{ mm}$$

$$k_1 = 35 \times 0.8 = 28, k_2 = 1, k_4 = 1, k_5 = 1$$

$$P_t = 100 A_{st} / b d = \frac{100 \times 523}{1000 \times 145} = 0.36\%$$

from fig-4 of pg: 38

$$f_x = 0.58 f_y \times \frac{A_{st \text{ req}}}{A_{st \text{ pro}}} = 177.64 \text{ mpa.}$$

$$\therefore k_3 = 1.7$$

$$\therefore \frac{4000}{145} \leq 28 \times 1 \times 1.7 \times 1 \times 1$$

$$\Rightarrow 27.58 \leq 47.6 \quad [\text{Hence OK}]$$

\therefore The slab is safe in deflection

TRAFFIC VOLUME ANALYSIS

DAY: MONDAY NAME OF THE NH-16 DIRECTION; TOWARDS GUNTUR
 DATE: 16/09/2019 SURVEY LOCAT NEAR KALLAM SPPING MILLS

TIME	APSRTC		PRIVATE BUSES	LCV	AUTO RICKSHA W	LORRY	CAR	2 WHEELERS (BIKES)	BICYCLES	TOTAL VEHICLES	PCU VALUES FOR EACH HOUR
	EXPRESS	ORDINARY									
10:30-10:45	12	5	5	4	22	30	79	99	2	258	249
10:45-11:00	10	9	4	11	18	34	66	125	5	282	265
11:00-11:15	18	14	9	18	10	20	85	113	8	295	293
11:15-11:30	22	11	7	4	29	29	58	123	4	287	280
11:30-11:45	26	12	11	19	24	34	72	134	3	335	341
11:45-12:00	10	5	5	25	20	44	68	155	7	339	311
12:00-12:15	13	19	6	14	18	33	72	162	1	338	317
12:15-12:30	18	11	8	10	10	19	77	119	5	277	266
PCU VALUES	2.2	2.2	2.2	1	0.5	2.2	1	0.4	0.7		

CALCULATIONS:

249 = (12X2.2)+(5X2.2)+(5X2.2)+(4X1)+(22X0.5)+(30X2.2)+(79X1)+(99X0.4)+(2X0.7)

265 =

293 =

280 =

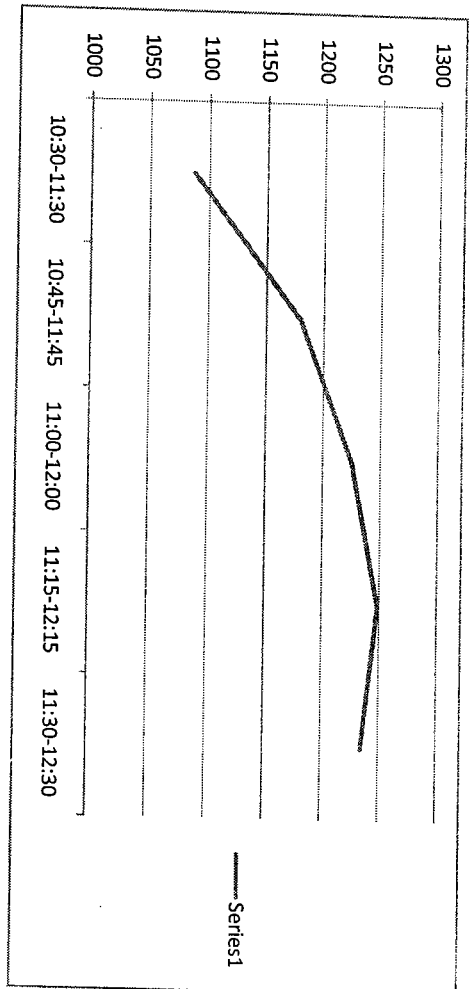
341 =

311 =

317 =

266 =

TIME	TOTAL PCU PER HOUR
10:30-11:30	1088
10:45-11:45	1180
11:00-12:00	1225
11:15-12:15	1249
11:30-12:30	1235



PEAK HOUR

FACTOR =

$\frac{\text{Peak hour volume}}{(60/15) * \text{Max volume at 15 min at peak hour}}$

Peak hour volume = 1249
 Max volume at 15 min at peak hour = 341 (from 11:30-11:45)

time Intreval	peak volume in PCU
11:15-11:30	280
11:30-11:45	341
11:45-12:00	311
12:00-12:15	317

$$= \frac{1249}{4 * 341}$$

$$= 0.92$$

Result:- peak hour volume is found for a time 11:15-12:15 and peak hour factor is 0.92